





Katrien Antonio



Roel Henckaerts

Paper will appear in **Insurance: Mathematics and Economics**.

[Henckaerts et al., 2018]



SAJ



[github.com/henckr/distRforest](https://github.com/henckr/distRforest)

[Henckaerts et al., 2021]



NAAJ

Page 2

[Henckaerts et al., 2022]



Expert Syst. Appl.



[github.com/henckr/maidrr](https://github.com/henckr/maidrr)

[Henckaerts & Antonio, 2022]



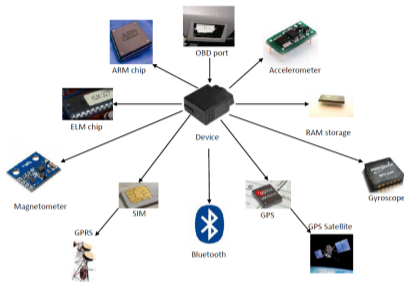
IME

- Denote for policyholder  $i$  in a given policy period:
  - $e_i$ : exposure-to-risk
  - $N_i$ : number of claims filed during the exposure period
  - $L_i$ : total loss amount reported during the exposure period.
- The **pure premium**  $\pi_i$ :

$$\pi_i = \mathbb{E} \left[ \frac{L_i}{e_i} \right] \stackrel{\text{indep.}}{=} \mathbb{E} \left[ \frac{N_i}{e_i} \right] \times \mathbb{E} \left[ \frac{L_i}{N_i} \mid N_i > 0 \right] = \underbrace{\text{Freq}_i}_{\text{frequency}} \times \underbrace{\text{Sev}_i}_{\text{severity}}$$

- Build  $f(\text{risk factors})$  to predict frequency and severity, respectively.

Products: **usage-based insurance (UBI)**  
**pay-as-you-drive (PAYD)**  
**pay-how-you-drive (PHYD)**



- **Telematics** is the integrated use of **tele**communications and **informatics**.
- Black-box device is installed in the vehicle.
- **Real driving behavior** is monitored.
- Very often targets **young drivers**.

# Risk factors for motor insurance pricing



Static, demographic data



License age



Car make/model

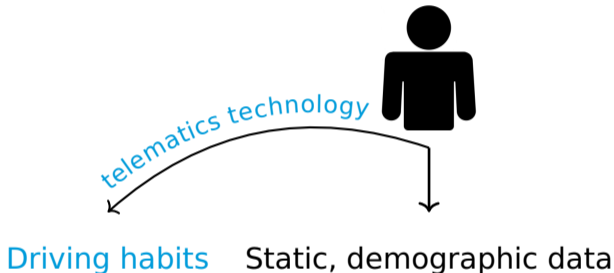


Type of fuel



Postal code

# Risk factors for motor insurance pricing



Mileage



Travel time

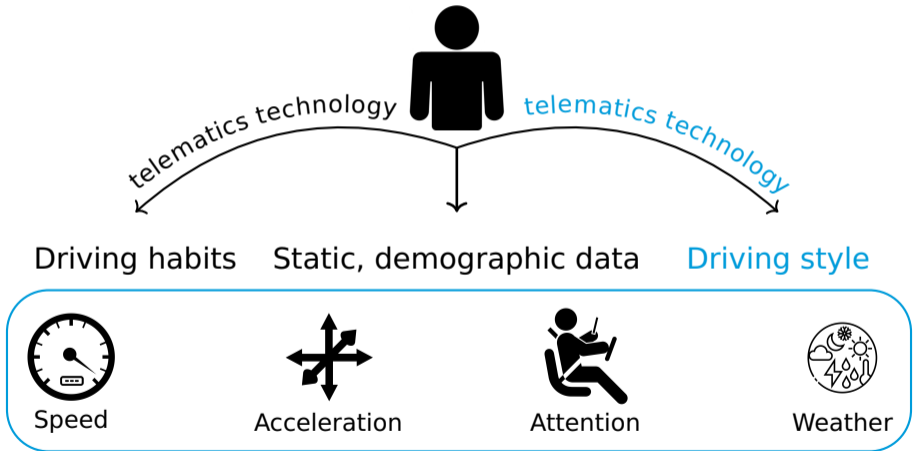


Time slot

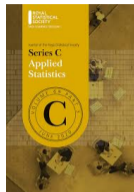


Road type

# Risk factors for motor insurance pricing



- Verbelen, Antonio & Claeskens (2018, JRSS C):
  - claim frequency models with classic, static features and driving habit information
  - compositional data and their use in GAMs.
- Wüthrich (2017, EAJ), Gao & Wüthrich (2018, EAJ), Gao et al. (2019, SAJ) and more papers:
  - the construction of  $v - a$  **heatmaps from GPS signals**
  - feature-engineering on these heatmaps
  - use of these features in claim frequency models.



- Denuit, Guillen & Trufin (2019, Annals of Actuarial Science) on **Multivariate credibility modelling for usage-based motor insurance pricing with behavioural data.**
- Grumiau, Mostoufi, Pavlioglou & Verdonck (2020, Risks) on **Address identification using telematics: an algorithm to identify dwell locations.**
- Banghee So, J.-P. Boucher & E. Valdez (2021, Risks) on **Synthetic dataset generation of driver telematics.**



Open Access    Preprint Paper    Article

## Address Identification Using Telematics: An Algorithm to Identify Dwell Locations

by  Christopher Grumiau <sup>1</sup>  Mina Mostoufi <sup>1,\*</sup>  Solon Pavlioglou <sup>1,\*</sup>  and  Tim Verdonck <sup>2,3</sup> 

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Risks 2020, 8(3), 92; <https://doi.org/10.3390/risks8030092>

Received: 16 June 2020 / Revised: 7 August 2020 / Accepted: 21 August 2020 / Published: 1 September 2020

(This article belongs to the Special Issue Data Mining in Actuarial Science: Theory and Applications)

Managerial insights, based on Carbone & Taub (2018) **UBI insurance is not usage-based. Sorry, not sorry!**

- In 2017, 14 million policies sent telematics data to insurers around the world.
- However, less than 9 percent of the global insurance telematics policies were characterized by **usage-based pricing**.
- **Use of driving data in pricing:**
  - \* use driving score at underwriting stage
  - \* propose tailored renewal price (with discounts, or discounts + surcharges)
  - \* usage-based, i.e. charge price for period of coverage based on how policyholder behaves during this period, and avoid **premium leakage**.

Our focus in this talk:

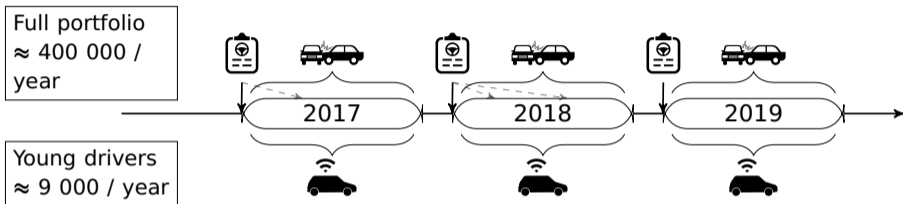
- How to use driving behavior (i.e. habits + style) to **update** a baseline **tariff** (with only self-reported characteristics)?
- What is the **added value** of telematics for pricing via risk classification?
- Managerial insights? Impact on retention rates, profit?


Focus on **frequency, severity and churn models** in the presence of static self-reported characteristics as well as telematics collected data.

Aim for an **explainable** updating mechanism.


# Data and methodology

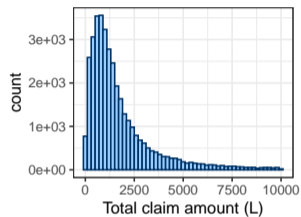
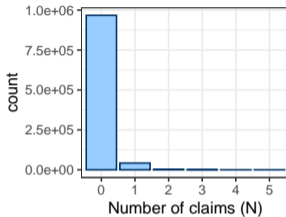
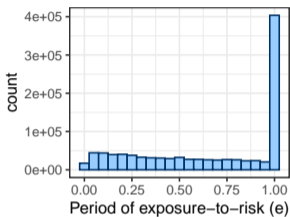
# Motor third party liability (MTPL) portfolio



 Policy information at the start of the policy period, subject to possible changes during the policy period (e.g., new vehicle).

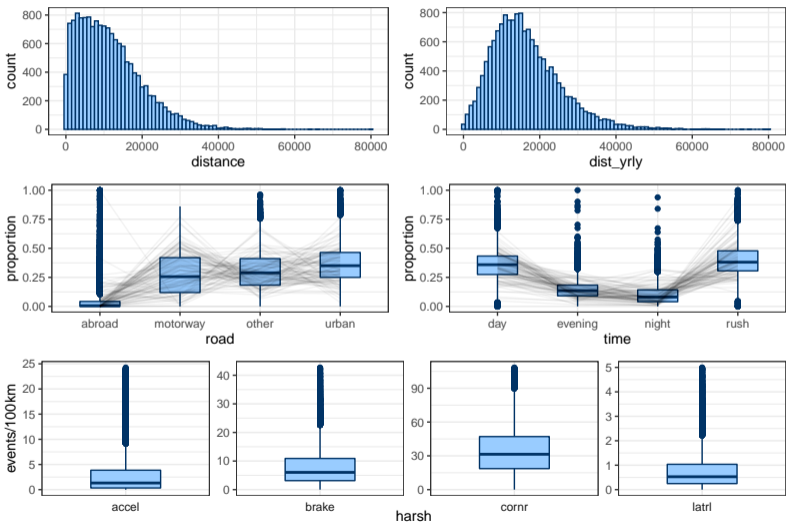
 Claims reported (68 196 in total).

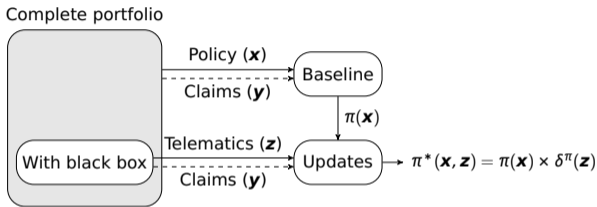
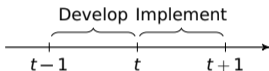
 Driving behavior (only for drivers < 26 years at underwriting time, 308M kilometers driven in total).



Policy information with **self-reported** risk characteristics:

- **driver**: age, experience, additional young drivers, etc.
- **payments**: frequency and SEPA indicator
- **geographical**: postal code and mosaic segment
- **vehicle**: age, weight, value, power, fuel, make, etc.





The idea:

- charge baseline tariff  $\pi(\mathbf{x})$  at  $t$
- ex post, multiplicative update  $\delta^\pi(\mathbf{z})$  at  $t + 1$ , based on driving data in  $[t, t + 1]$ .



- Predictive models for the **complete portfolio** using traditional features  $\mathbf{x}$ 
  - claim frequency *and* severity → **tariff**
  - customer churn prediction → client **retention** analysis.
- Stochastic gradient boosting (Friedman, 2002) with the following **assumptions**:

	Distribution	Prediction $f(\mathbf{x})$	Loss function $D(y, f(\mathbf{x}))$
Claim frequency	$N \sim \text{Poisson}$	$\mathbb{E}(N   \mathbf{x}, e)$	$\frac{2}{n} \sum_{i=1}^n \left[ y_i \ln \left\{ \frac{y_i}{f_i} \right\} - \{y_i - f_i\} \right]$
Claim severity	$L/N \sim \text{gamma}$	$\mathbb{E}(L/N   \mathbf{x})$	$\frac{2}{\sum_i N_i} \sum_{i=1}^n N_i \left[ \frac{y_i - f_i}{f_i} - \ln \left\{ \frac{y_i}{f_i} \right\} \right]$
Customer churn	$C \sim \text{Bernoulli}$	$\mathbb{E}(C   \mathbf{x})$	$-\frac{1}{n} \sum_{i=1}^n \left[ y_i \ln \{f_i\} + (1 - y_i) \ln \{1 - f_i\} \right]$

- Parameter **tuning**:

H2O random grid search + 5-fold cross-validation (LeDell et al., 2020).

- Enforce the **balance property** by scaling predictions (for the young drivers):

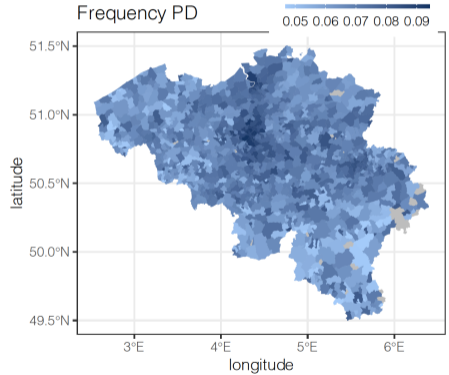
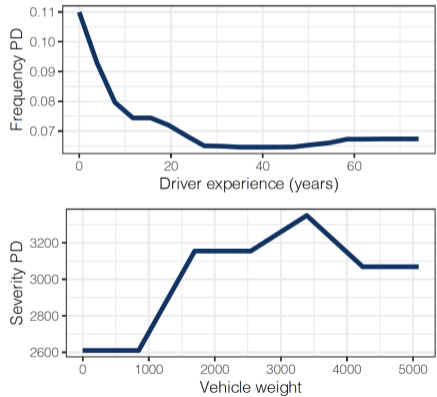
$$\sum_{i=1}^n f_i = \sum_{i=1}^n y_i$$

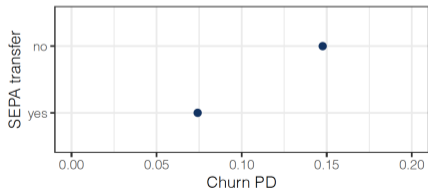
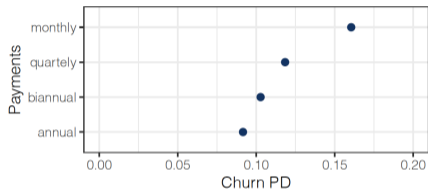
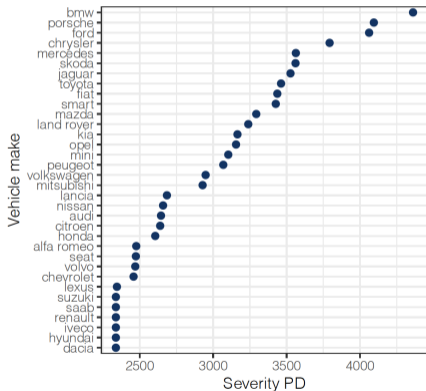
automatically fulfilled for GLMs with canonical link

see e.g. Wüthrich (2020).

Rank	Claim frequency		Claim severity		Customer churn	
	Feature	%	Feature	%	Feature	%
1	geo_postcode	34.72	veh_weight	23.21	paym_split	43.48
2	driv_experience	14.08	veh_make	21.37	geo_postcode	11.67
3	driv_seniority	8.52	geo_postcode	10.54	veh_age	9.85
4	veh_make	6.25	veh_segment	10.48	paym_sepa	9.44
5	geo_mosaic	5.85	geo_mosaic	6.59	driv_seniority	6.90
6	veh_fuel	5.09	driv_seniority	5.83	veh_make	3.43
7	veh_segment	4.66	veh_value	3.50	driv_experience	2.85
8	paym_split	3.91	veh_age	3.44	geo_mosaic	2.45
9	driv_add_younger26	3.29	driv_experience	2.98	driv_age	2.43
10	driv_age	2.75	driv_add_younger26	2.91	veh_use	1.99
$\Sigma$		89.12		90.86		94.48

# Insights in the optimal GBMs (cont.)

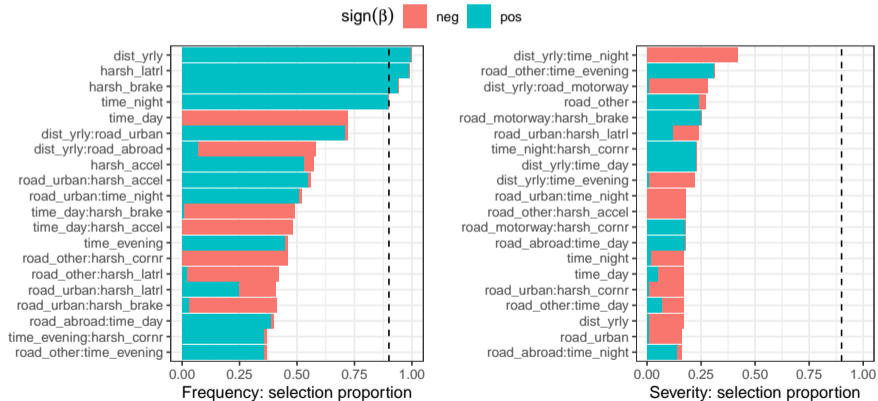




# Updating pricing with driving behavior



# Telematics feature selection with LASSO



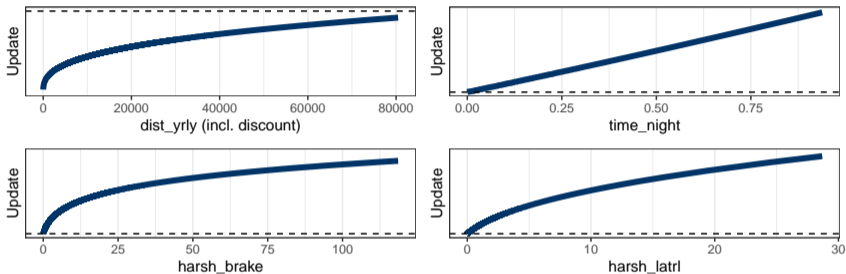
- Let  $\mathbf{z}^* \in \mathbb{R}^4$  denote {dist\_yrly, harsh\_latrl, harsh\_brake, time\_night}.
- Log-link Poisson GLM with offset for **claim frequency**:

$$\ln[\mathbb{E}(N | \mathbf{x}, \mathbf{z}^*)] = \ln[\mathbb{E}(N | \mathbf{x}, e)] + \beta_0 + \sum_{j=1}^4 \beta_j \log(z_j^* + 1)$$

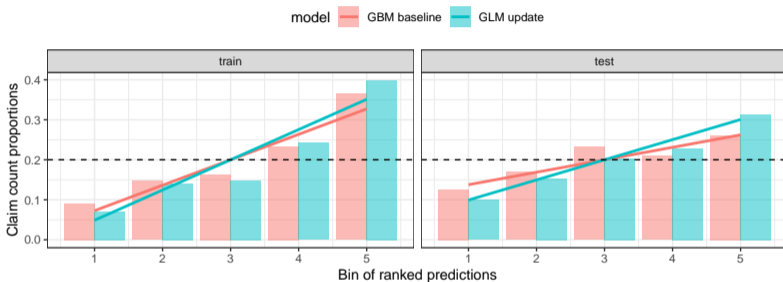
$$\mathbb{E}(N | \mathbf{x}, \mathbf{z}^*) = \mathbb{E}(N | \mathbf{x}, e) \times \exp(\beta_0) \times \prod_{j=1}^4 (z_j^* + 1)^{\beta_j}.$$

Updated prediction is **multiplicative** in the following terms:

- baseline GBM prediction  $\mathbb{E}(N | \mathbf{x}, e)$  for a policyholder with risk characteristics  $\mathbf{x}$
- overall discount factor  $\exp(\beta_0) \approx 2\%$
- update  $(z_j^* + 1)^{\beta_j}$  from each telematics feature  $z_j^*$ .

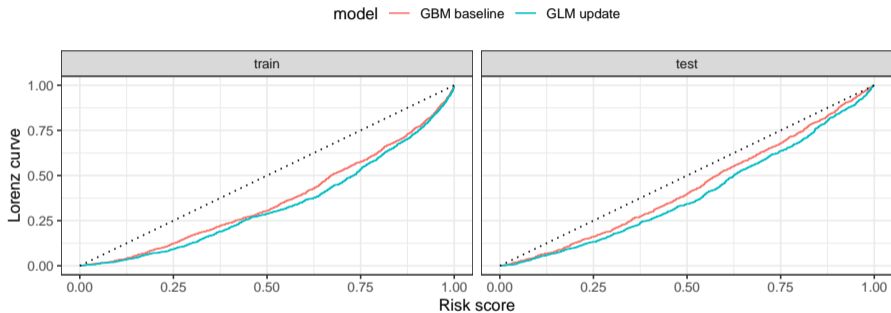


- Mileage + discount remains  $< 1$ .
- Penalty once night driving, harsh braking or lateral events are registered.
- Safe driving is the key to earn discounts!



Here we consider:

- $r_i^m = F_n(f^m(\mathbf{x}_i, \mathbf{z}_i^*))$  with  $F_n(\cdot)$  the ecdf
- $PC^m(s) = \frac{\sum_{i=1}^n N_i \mathbb{1}\{\frac{s-1}{5} < r_i^m \leq \frac{s}{5}\}}{\sum_{i=1}^n N_i}$  for  $s \in \{1, \dots, 5\}$ .



Here we consider:

- $$LC^m(s) = \frac{\sum_{i=1}^n N_i \mathbb{1}\{r_i^m \leq s\}}{\sum_{i=1}^n N_i} \text{ for } s \in [0, 1].$$

# Managerial insights

For the discussion of managerial insights, I refer to our paper:

- **adjust baseline churn**  $\rho(\mathbf{x})$  to  
 $\rho^*(\mathbf{x}, \delta^\pi) = \rho(\mathbf{x}) + \epsilon_\rho \cdot (\delta^\pi - 1) = \rho(\mathbf{x}) + \delta^\rho$ , with  $\epsilon_\rho$  the price elasticity
- study expected **profit and retention rate**

$$P = \frac{1}{n} \sum_{i=1}^n (1 - (\rho_i + \delta_i^\rho)) \cdot (\delta_i^\pi \pi_i - L_i) \quad R = \frac{1}{n} \sum_{i=1}^n 1 - (\rho_i + \delta_i^\rho)$$

- restrict penalties/discounts + redistribute  $\Rightarrow$  **fairness, solidarity, commercially appealing**

$$\delta_{lo}^\pi \leq \delta^\pi \leq \delta_{hi}^\pi$$

$$\sum_{i=1}^n (1 - \rho_i) \cdot \pi_i = \sum_{i=1}^n (1 - \rho_i) \cdot \alpha \cdot \delta_i^\pi \cdot \pi_i$$

Our paper puts focus on:

- a baseline pricing model with self-reported characteristics
- an explainable updating mechanism to incorporate driving behavioral information.

Added value of telematics for insurance pricing is studied from both a statistical and managerial perspective.

For more information, please visit:

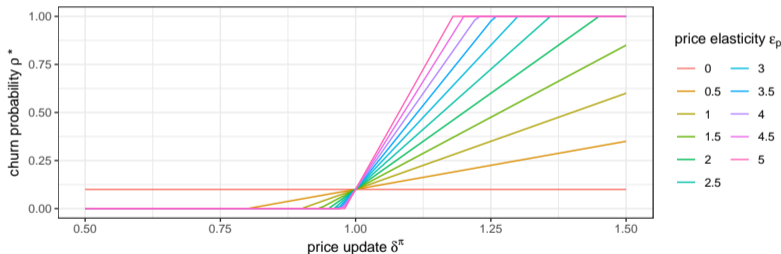
- draft of the paper, including complete set of references
- LRisk website, [www.lrisk.be](http://www.lrisk.be)
- my homepage <https://katrienantonio.github.io>.

Special thanks to

- the organizers
- the companies and funding agencies supporting/having supported my research lab: Ageas, Argenta, Atlas Copco, CNP Assurances, FWO, KU Leuven internal funds.

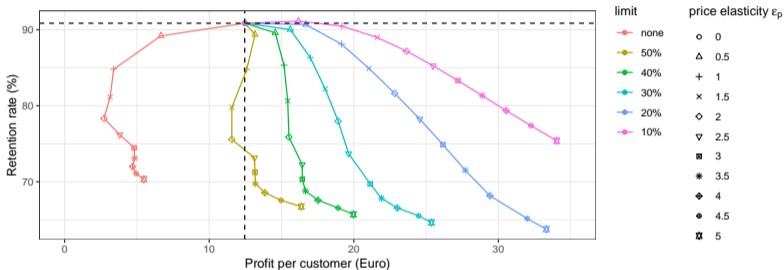
# Extra Sheets

- Adjust baseline churn via price **update**  $\delta^\pi$  and **elasticity** of demand  $\epsilon_p$ .
- $\rho^*(\mathbf{x}, \delta^\pi) = \rho(\mathbf{x}) + \epsilon_p \cdot (\delta^\pi - 1)$  for  $\rho(\mathbf{x}) = 0.1$  and  $\epsilon_p \in [0, 5]$ :



- $\rho^* = \rho$  when  $\delta^\pi = \pi^*/\pi = 1$  (no price change).
- Linear increases/decreases ( $\delta^\pi > 1$  /  $\delta^\pi < 1$ ) with slope  $\epsilon_p$ .

- Expected profits and retention rates under different scenarios:



- Stricter limits result in higher profits
- Profits increase with  $\epsilon_p$  at the cost of lower retention
- No limit results in lower profits than baseline (driven by low premiums on average)

- Maximize expected profit  $P$  while retaining a minimum proportion of the portfolio  $R^*$  :

$$\max_{\alpha} P(\alpha) = \frac{1}{n} \sum_{i=1}^n (1 - (\rho_i + \delta_i^{\rho})) \cdot (\alpha \delta_i^{\pi} \pi_i - L_i)$$

$$\text{subject to } R(\alpha) = \frac{1}{n} \sum_{i=1}^n 1 - (\rho_i + \delta_i^{\rho}) \geq R^*$$

$$\delta_{lo}^{\pi} \leq \delta^{\pi} \leq \delta_{hi}^{\pi}$$

- Implicit dependence of  $R$  on  $\alpha$  as  $\delta^{\rho} = \epsilon_{\rho} \cdot (\alpha \delta^{\pi} - 1)$ .
- Efficient frontier by varying  $R^*$  over a range of values and maximizing  $P(R^*)$  via  $\alpha$ .

# Efficient frontiers for $R^* \in [0.75, 0.9]$ under different scenarios

